

# Monitoring Distributed Streams using Convex Decompositions

Arnon Lazerson, Izchak Sharfman, Assaf Schuster. Technion I.I.T. {lazerson,tsachis,assaf}@cs.technion.ac.il

Daniel Keren. Haifa University. dkeren@cs.haifa.ac.il

Minos Garofalakis, Vasilis Samoladas. Technical University of Crete. {minos,vsam}@softnet.tuc.gr

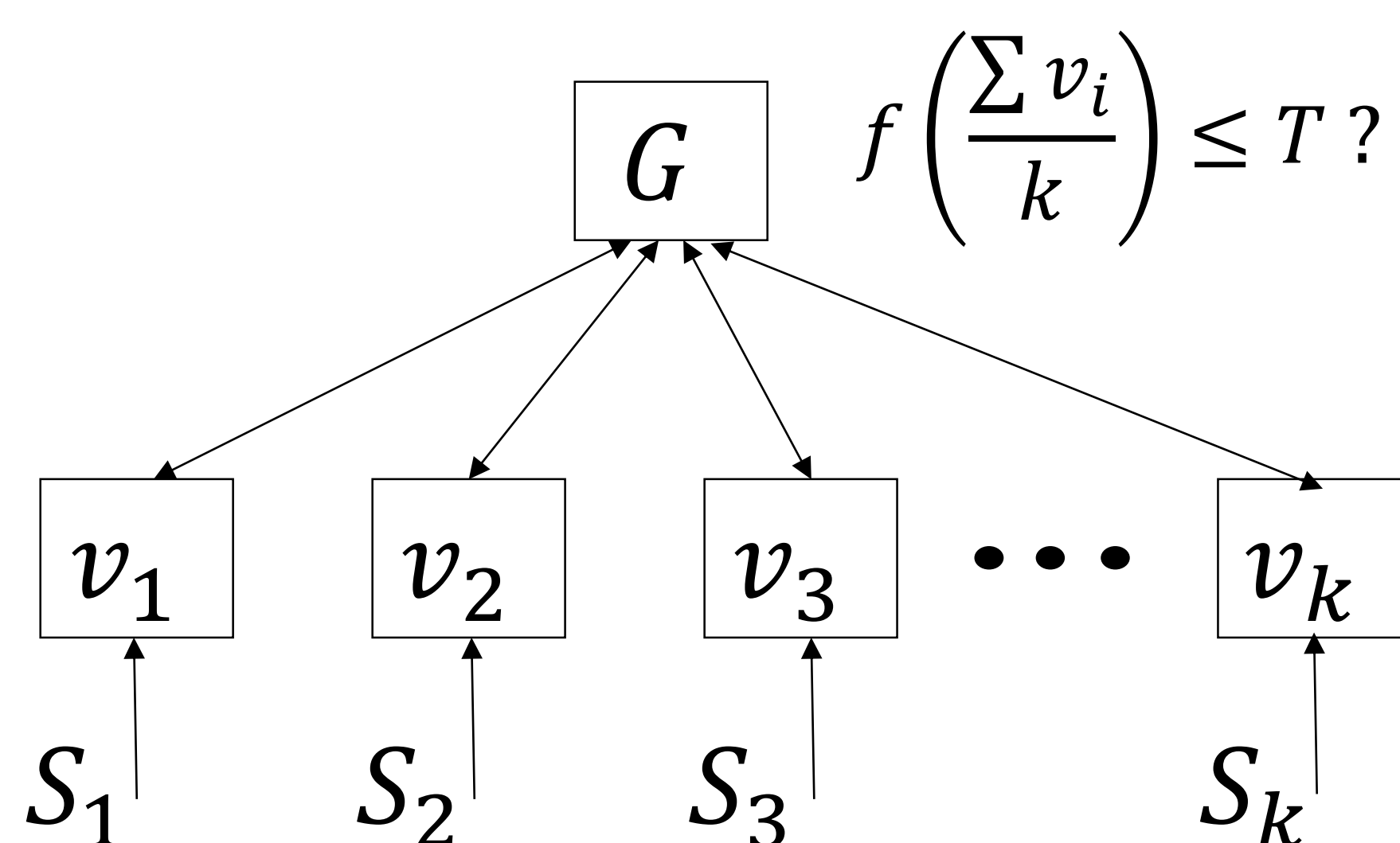
## Background

Large-scale monitoring applications rely on continuous tracking of complex queries over distributed data streams. Effective distributed stream processing solutions must be

- Space efficient
- Time efficient
- **Communication efficient**

## Distributed Monitoring Model

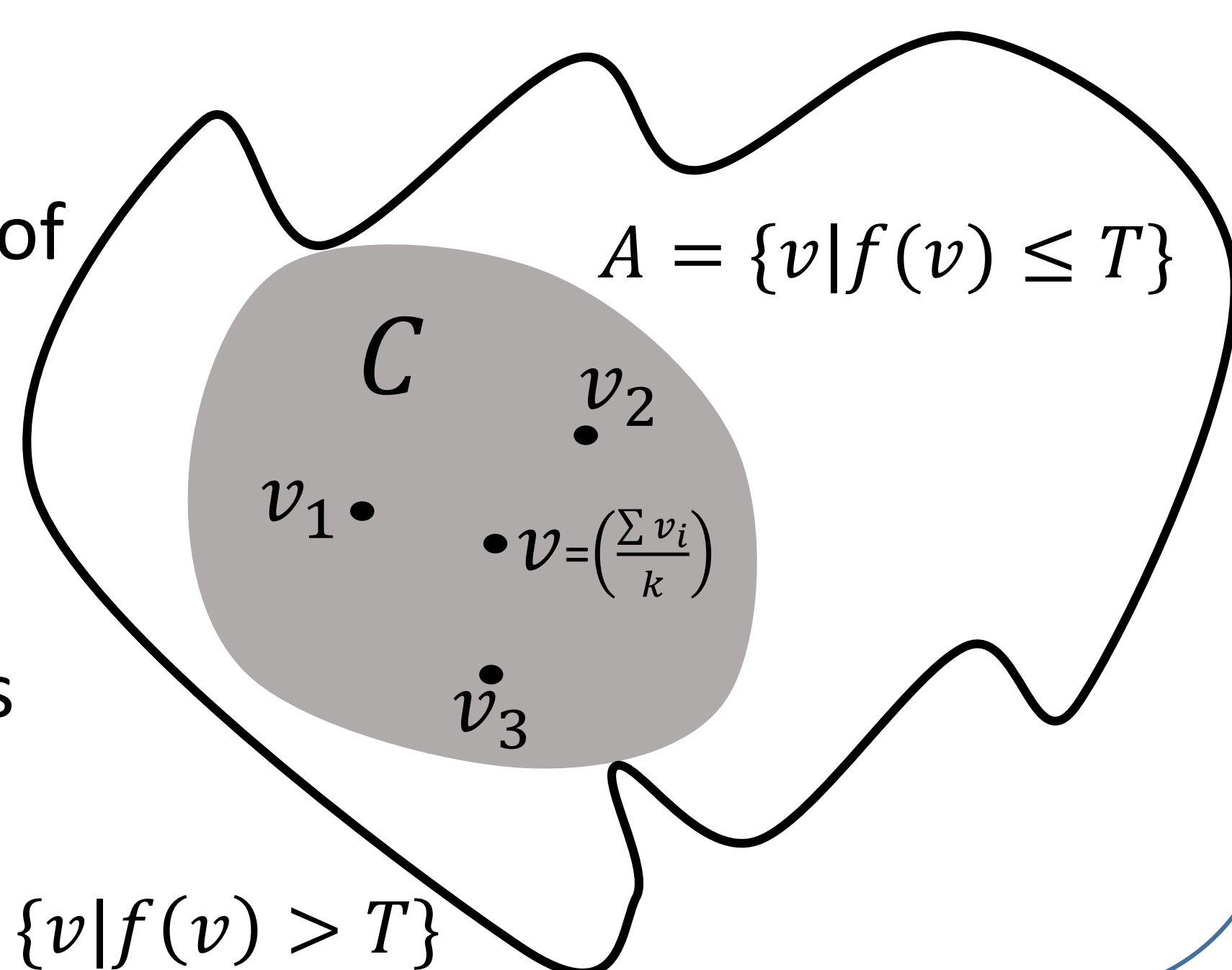
Distributed streams  $S_i$  continuously update the local vectors  $v_i$ . The coordinator  $G$  must issue an alert when the global condition  $f\left(\frac{\sum v_i}{k}\right) \leq T$  is breached.



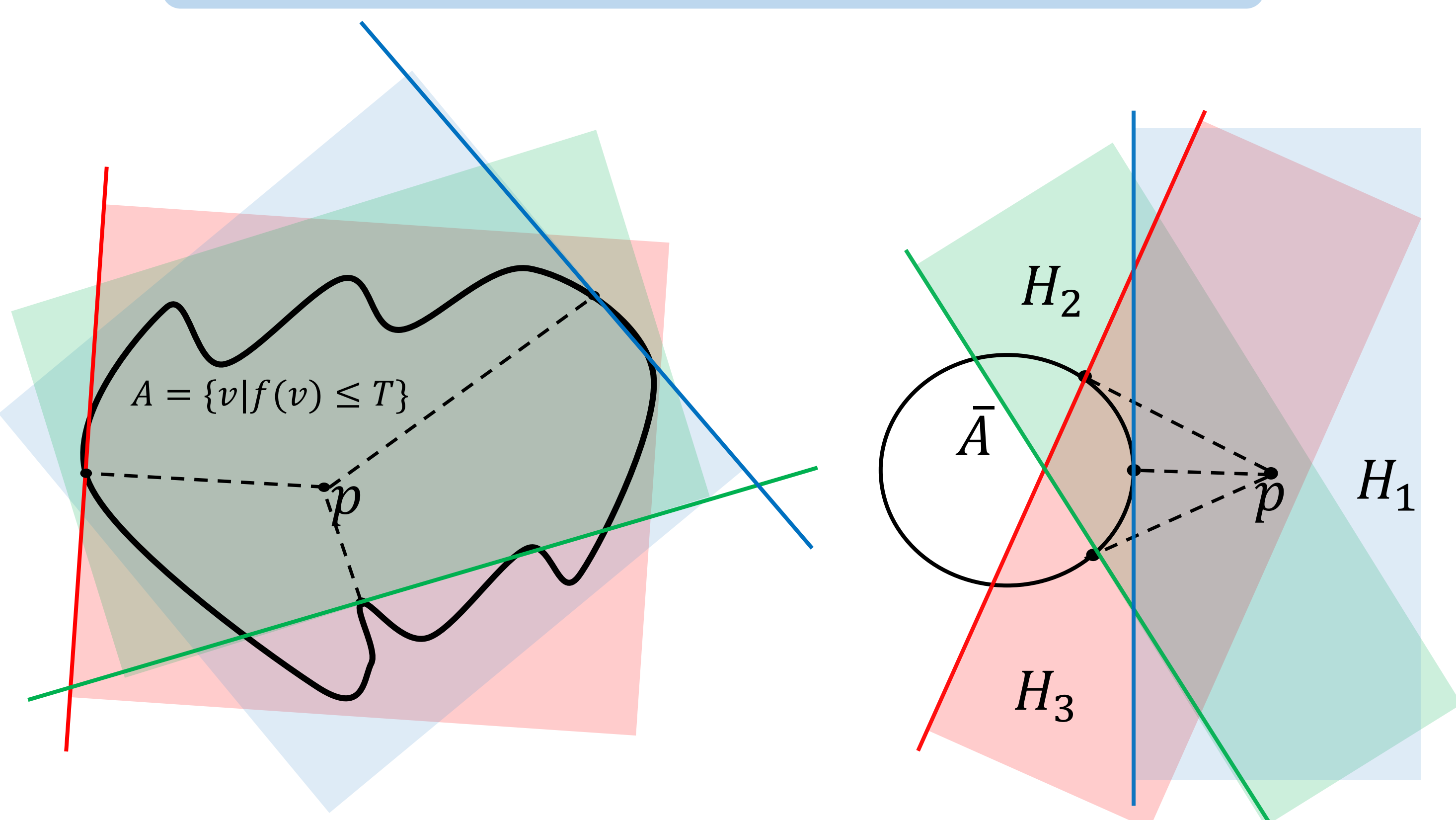
## Geometric Monitoring

The set  $A = \{v | f(v) \leq T\}$  is called the *admissible region*.  $C$  is a *convex* subset of  $A$ .  $C$ 's convexity guarantees that if  $v_1, v_2 \dots v_k \in C$ , then  $v = \left(\frac{\sum v_i}{k}\right) \in C \subseteq A$ . Node  $i$  stays silent as long as  $v_i \in C$ .

$$\bar{A} = \{v | f(v) > T\}$$

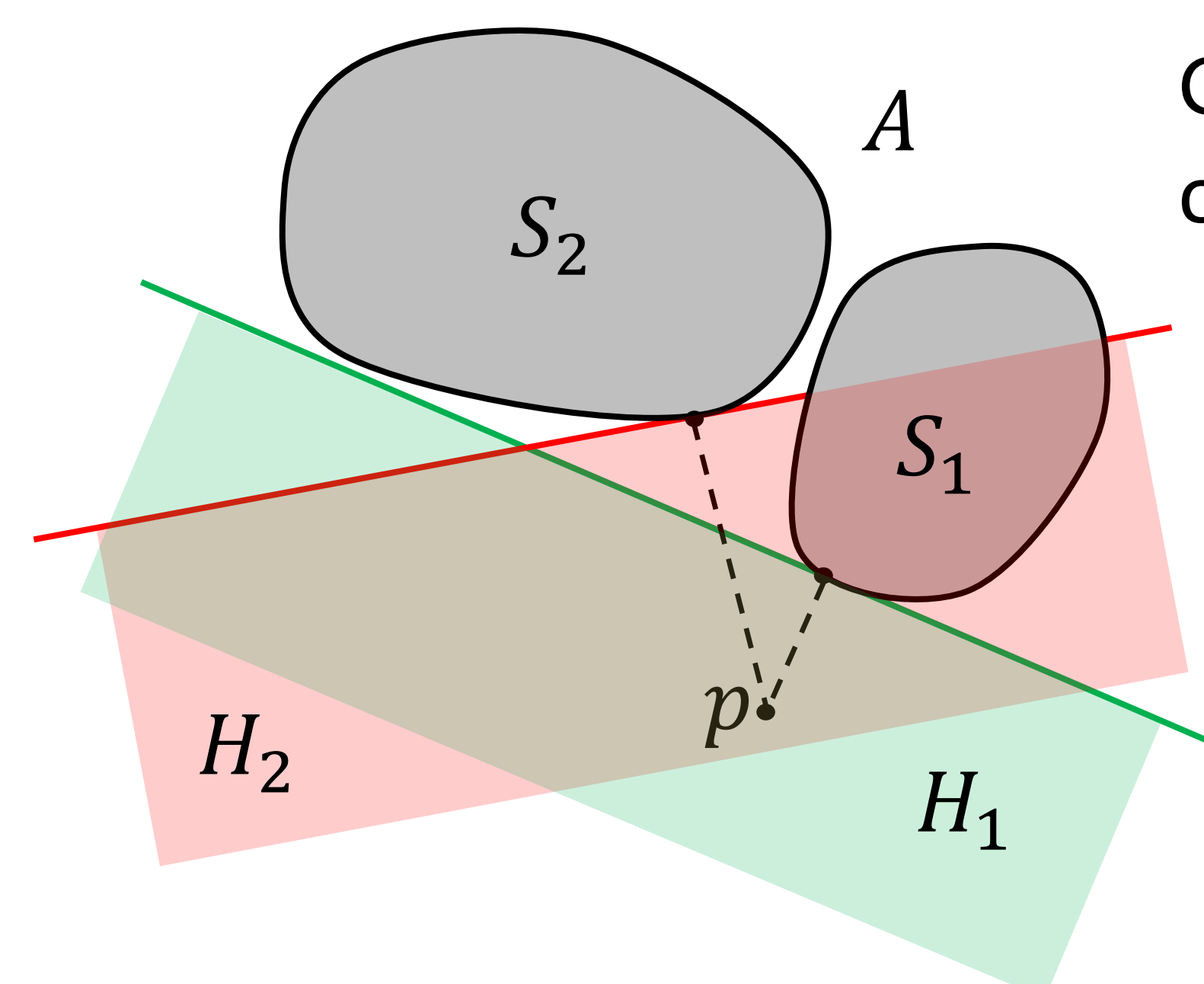


## Using half-spaces to construct C



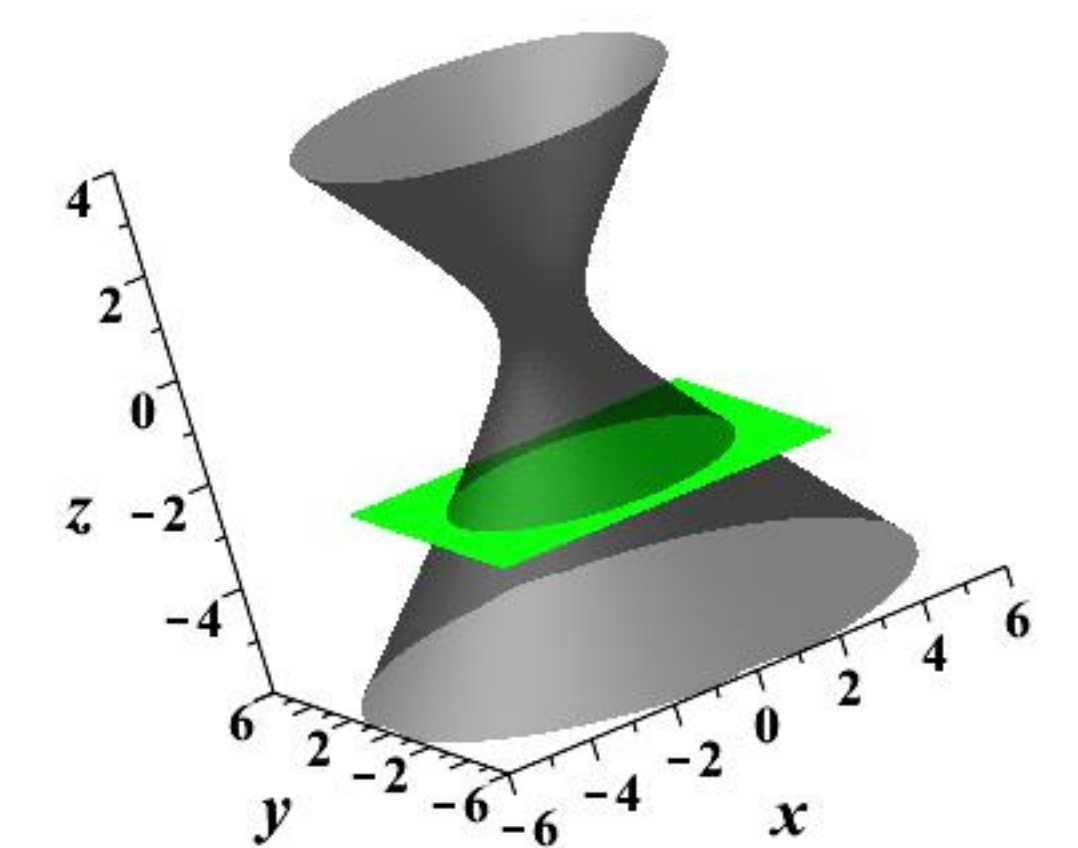
Left: A convex subset of  $A$  containing a point  $p$  can be created in the following manner: for each point  $q$  on the boundary of  $\bar{A}$  take the half-space orthogonal to  $pq$  containing  $p$ . Then take the intersection of these half-spaces. Right: When  $\bar{A}$  is convex this method yields a non-optimal  $C$ . Clearly,  $H_1$  is a better convex subset (it contains  $H_1 \cap H_2 \cap H_3$ ).

## Convex Decomposition



General case: *convex decomposition* of  $\bar{A}$ , but avoid **redundancy!**

If  $\bar{A}$  is the hyperboloid, it can be decomposed to a infinite union of (convex) parallel discs.



If  $\bar{A}$  is the union of the two convex sets,  $S_1$  and  $S_2$ , and  $H_1$  separates  $p$  from  $S_2$ , there is no need to intersect with  $H_2$ , and  $C$  can be defined as  $H_1$

## Monitoring the median

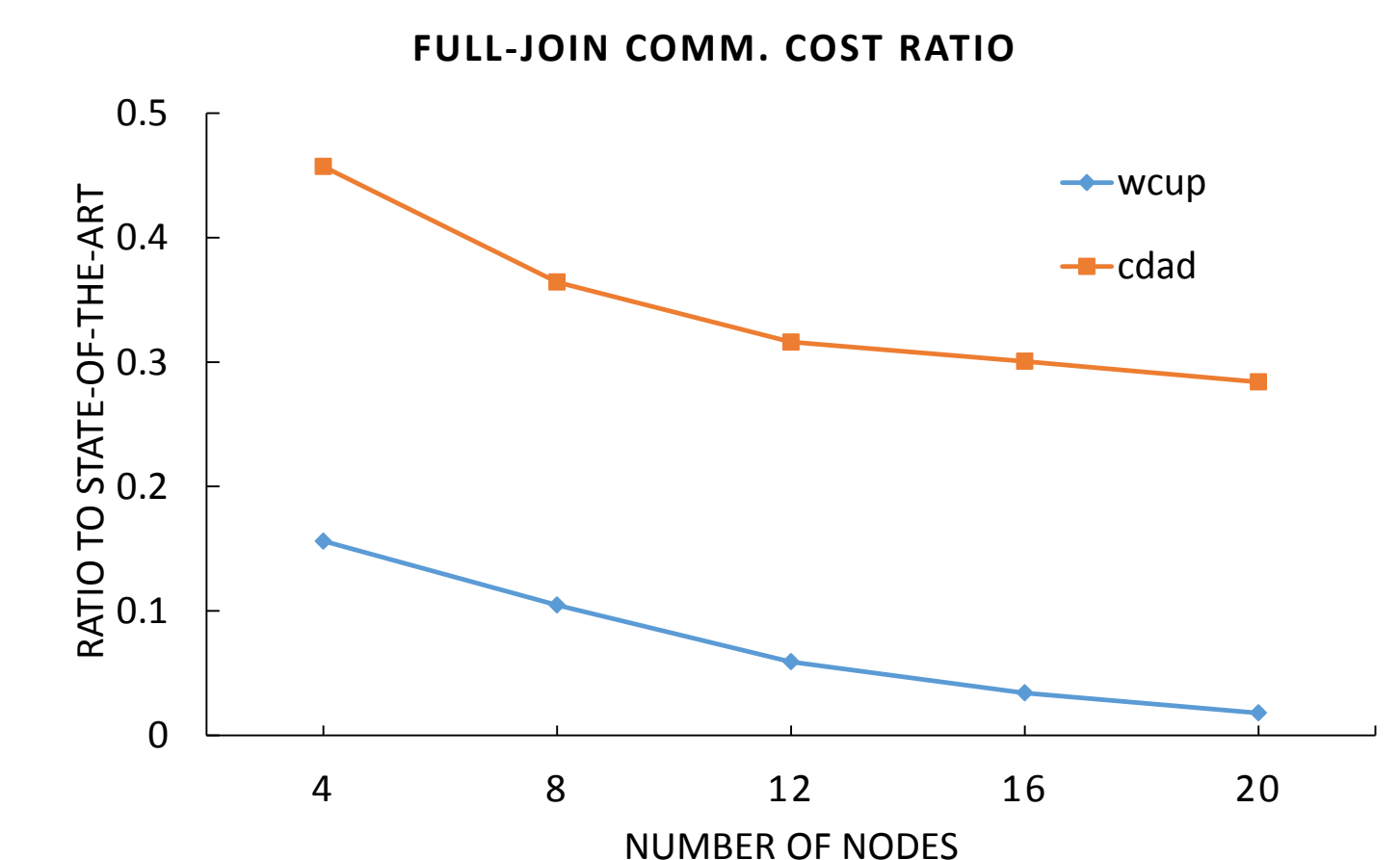
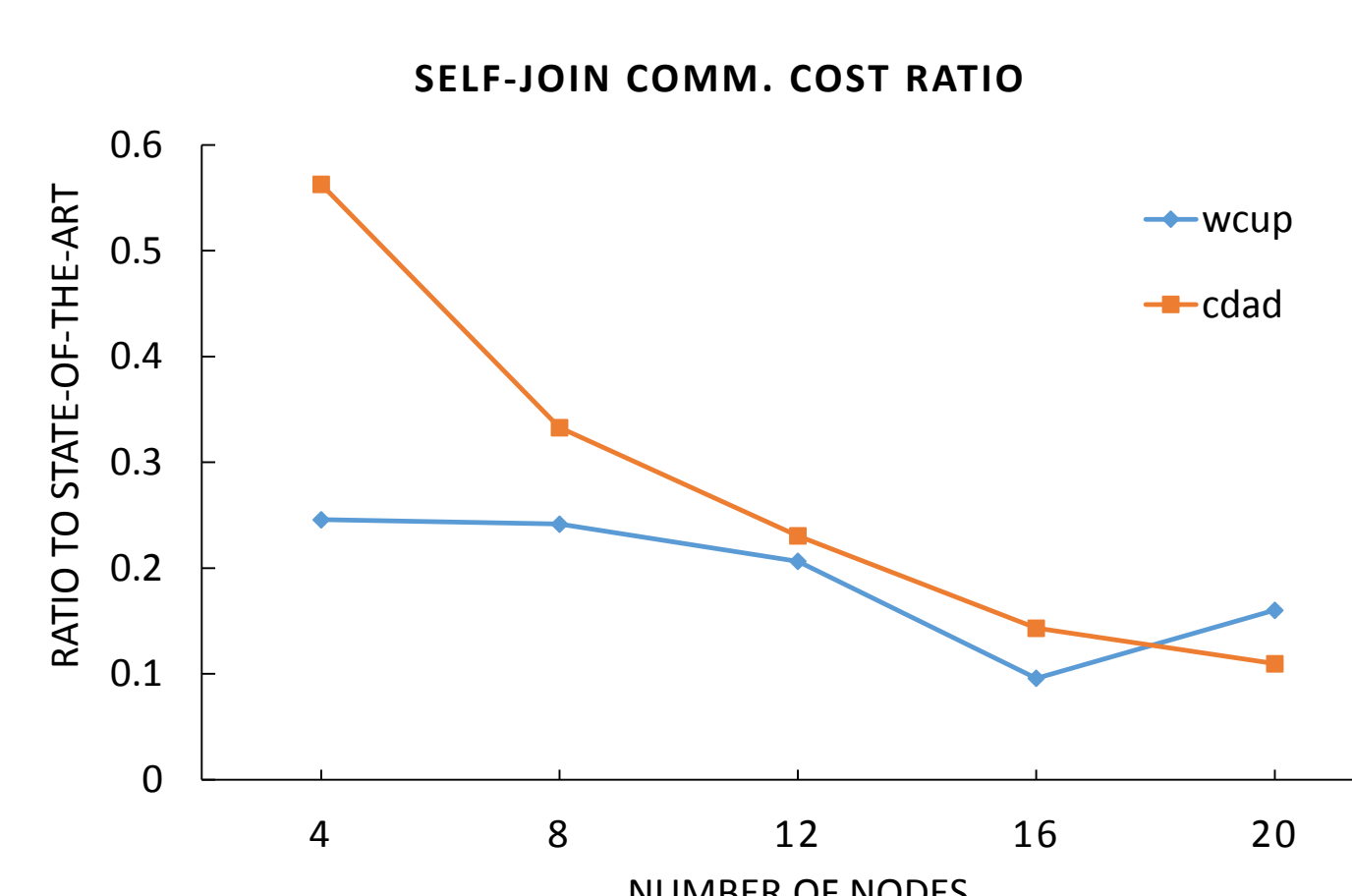
- We wish to monitor  $med(x_1, x_2, x_3) > 0$
  - $A$  is not convex. The vectors  $(1, 1, -11)$ ,  $(1, -11, 1)$ ,  $(-11, 1, 1)$  are in  $A$ , but their average  $(-3, -3, -3)$  is not.
  - We partition the complement  $\bar{A}$  to convex subsets:  $(x_1, x_2 \leq 0)$ ,  $(x_1, x_3 \leq 0)$ ,  $(x_2, x_3 \leq 0)$
  - This is a non-redundant decomposition (can be proved)
  - It can be generalized to any dimension.
- \* The number of sets in the decomposition is exponential, but a simple trick allows to check whether a point belongs to the  $A$  in  $n \log(n)$  time, where  $n$  is the dimension.

## Sketches

- AGMS sketches provide summary of the data using a  $k \times l$  matrix  $M$ .
- To approximate the result of range, self-join and full-join queries the median operator is applied to a vector constructed either by taking the norm squared of each matrix row, or by taking the inner-product of the rows of two sketch matrices (median of a *quadratic* function).
- This is more complicated than the linear median case, but can be solved.

## Evaluation

The CD method was tested on two real data sets for self-join and full-join queries using sketches, it yielded substantial improvement over the state-of-the-art.



Communication cost (bytes sent) relative to state-of-the-art for varying number of nodes over two datasets. Left: self-join. Right: full-join (smaller is better).